

BSM 6-Line and Multiple integrals and Laplace Transforms

Programme	B.Sc
Subject	Mathematics
Semester	V
University	Kuvempu University
Session	7

Double integration

Evaluation of double integrals under given limits

Recap of previous class

- Definition of line integral and basic properties
- Definition of double integrals and basic properties

Objectives:

1. Evaluation of double integrals under given limits
2. Examples on double integrals under given limits

Session outcomes

- To able to understand the double integration
- To able to understand properties of double integration
- To able to understand problems

Prerequisites

- Standard formulae of integration

Problems:

$$1) \int_0^a \int_0^b (x^2 + y^2) dx dy$$

$$2) \int_0^1 \int_0^2 (x + y) dy dx$$

$$3) \int_0^3 \int_1^2 (x^2 + 3y^2) dy dx$$

$$4) \int_0^1 \int_0^1 (x^2 + xy) dy dx$$

Session Summary:

- To solve double integration, which is useful in finding certain areas.
- The knowledge is a must before tackling double integrals

MCQ :

1) $\int_0^{\frac{\pi}{2}} \int_{\frac{\pi}{2}}^{\pi} \cos(x + y) dx dy$ is equal to

A. 2

B. 1

C. -1

D. -2

Ans : A

MCQ :

2. $\int_1^2 \int_0^{3y} y dy dx$ is equal to

A. 3

B. 5

C. 7

D. 9

Ans : C

MCQ

3) $\int_0^1 \int_0^{\sqrt{1-y^2}} y dy dx$ is equal to

A. 3

B. $\frac{1}{3}$

C. 2

D. $\frac{1}{2}$

Ans : B

MCQ :

4. Solution of $\int_1^2 \int_0^x \frac{dx dy}{x^2 + y^2}$

A. $\frac{1}{4} \log 2$

B. $\frac{1}{2} \log 4$

C. $\frac{\pi}{2} \log 4$

D. $\frac{\pi}{4} \log 2$

Ans : D

References:

- Manjunath, B. V. and Nandeeshkumar(2018). A textbook of B.Sc Mathematics. College book house, Bangalore.
- Ranganath G. K (2012). A textbook of B.Sc Mathematics (Sixth). S. Chand, New Delhi.